

Homework 1

Stat 345 - Spring 2020

Problem 1

For each of the following experiments, describe the sample space S

- a) Picking 2 marbles, one at a time, from a bag that contains many yellow and green marbles
- b) Getting two odd faces from rolling two dice
- c) Count the proportion of defectives items in a shipment
- d) Count the number of hail damaged spots on some car

Problem 2

Pick a card from the standard deck of 52 cards. Consider the following events:

$$A = \{\text{card has a Red Suit}\}$$

$$B = \{\text{card is a Heart}\}$$

$$C = \{\text{card is a Queen}\}$$

$$D = \{\text{card is a King}\}$$

Describe these events in terms of problem.

a) $A \setminus B$

b) $(B \cap A) \cup (A \cap B^c)$

c) $(C \cup D)^c$

d) $(A \cup B) \cap C$

e) $(C \cup D) \cap B$

Problem 3

Jane has 11 friends. She is planning to meet with some of her friends each day of a certain week, Thursday through Sunday (one friend per day).

- How many possibilities are there for Jane's schedule for that week, if she is not willing to meet with the same friend more than once?
- How many possibilities are there for Jane's schedule for that week, if she is willing to meet with the same friend more than once, but not twice in a row (or more)?

Problem 4

You have 7 rock music CDs, 5 indie music CDs, and 2 pop music CDs.

- In how many ways can you arrange them?
- In how many different ways can you arrange them so that the CDs of the same type are contiguous?
- Suppose that you want to give your *rock music CDs* to your friends. You want to give 3 to Max, 2 to John, and 2 to Alice. In how many ways you can do that?

Problem 5

From a group of 9 biologists and 5 chemists, a group consisting of 3 biologists and 2 chemists is to be formed. In how many ways can this be done if

- any biologist and any chemist can be included?
- one particular chemist must be in the group?
- three particular biologists cannot be in the group?

Problem 6

Use *R* statistical software (include your code) to make a well labeled plot $y = \left(1 + \frac{1}{n}\right)^n$.

Show on the plot that y approaches e for large n . This will illustrate that

$$\lim_{n \rightarrow \infty} \left(1 + \frac{1}{n}\right)^n = e$$

Bonus problem

You want to buy 7 cakes from a local bakery. The store has 4 types of cakes: chocolate, apple, cinnamon, and coconut cakes. How many different selections can you make? Note that cakes of the same type are considered indistinguishable.